

## Are you getting the whole picture?

- Compact Camera FOV $=50 \times 35^{\circ}$



# Are you getting the whole picture? 

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- Compact Camera FOV $=50 \times 35^{\circ}$
- Human FOV $=200 \times 135^{\circ}$



## Are you getting the whole picture?

- Compact Camera FOV $=50 \times 35^{\circ}$
- Human FOV $=200 \times 135^{\circ}$
- Panoramic Mosaic $=360 \times 180^{\circ}$



## Panorama

## A wide-angle representation of the scene



Panorama: Cinema for the early $19^{\text {th }}$ century


Burford's Panorama, Leicester Square, London, 1801

## Panoramas with wide-angle optics

http://www.0-360.com


AF DX Fisheye-NIKKOR 10.5mm f/2.8G ED


## Rotation cameras

- Idea
- rotate camera or lens so that a vertical slit is exposed
- Swing lens
- rotate the lens and a vertical slit (or the sensor)
- typically can get 110-140 degree panoramas
- Widelux, Seitz, ...
- Full rotation
- whole camera rotates
- can get 360 degree panoramas
- Panoscan, Roundshot, ...



## Swing-lens panoramic images



## San Francisco in ruins, 1906

101 Ranch, Oklahoma, circa 1920

Flatback panoramic camera


## Disposable panoramic camera

 wide-angle lens, limited vertical FOV




## Stitching images to make a mosaic



## Stitching images to make a mosaic



- Given a set of images that should stitch together
- by rotating the camera around its center of perspective
- Step 1: Find corresponding features in a pair of image
- Step 2: Compute transformation from $2^{\text {nd }}$ to $1^{\text {st }}$ image
- Step 3: Warp $2^{\text {nd }}$ image so it overlays $1^{\text {st }}$ image
- Step 4: Blend images where they overlap one another
- repeat for $3^{\text {rd }}$ image and mosaic of first two, etc.


## Aligning images: Translation?



Translations are not enough to align the images


## A pencil of rays contains all views



Can generate any synthetic camera view as long as it has the same center of projection! mvom eseacen ... and scene geometry does not matter ...

## Reprojecting an image onto a different picture plane


the sidewalk art of Julian Beever

- the view on any picture plane can be projected onto any other plane in 3D without changing its appearance as seen from the center of projection


## Image reprojection



- The mosaic has a natural interpretation in 3D
- the images are reprojected onto a common plane
- the mosaic is formed on this plane
- mosaic is a synthetic wide-angle camera


## Which transform to use?



Translation


2 unknowns

Affine


6 unknowns

Perspective


8 unknowns

## Homography

- Projective mapping between any two PPs with the same center of projection
- rectangle should map to arbitrary quadrilateral
- parallel lines aren't
- but must preserve straight lines is called a Homography
$\underset{\mathbf{p}^{\prime}}{\left[\begin{array}{c}w \boldsymbol{x}^{\prime} \\ w y^{\prime} \\ w\end{array}\right]}=\underset{\underline{\underline{p}}}{\left[\begin{array}{lll}h_{11} & h_{12} & h_{13} \\ h_{21} & h_{22} & h_{23} \\ h_{31} & h_{32} & h_{33}\end{array}\right]\left[\begin{array}{c}x \\ y \\ 1\end{array}\right]}$
- To apply a homography H
- compute $\mathrm{p}^{\prime}=\mathrm{Hp} \quad$ (regular matric multiply)
- convert $p^{\prime}$ from homogeneous to image coordinates [ $\mathrm{x}^{\prime}, \mathrm{y}^{\prime}$ ] (divide by w)



## Homography from mapping quads



Figure 2.8: Quadrilateral to quadrilateral mapping as a composition of simpler mappings.

Fundamentals of Texture Mapping and Image Warping Paul Heckbert, M.Sc. thesis, U.C. Berkeley, June 1989, 86 pp. http://www.cs.cmu.edu/~ph/texfund/texfund.pdf

## Homography from $n$ point pairs ( $x, y ; x^{\prime}, y^{\prime}$ )

- Multiply out

$$
\begin{aligned}
& w x^{\prime}=h_{11} x+h_{12} y+h_{13} \\
& w y^{\prime}=h_{21} x+h_{22} y+h_{23} \\
& w=h_{31} x+h_{32} y+h_{33}
\end{aligned}
$$

- Get rid of w

$$
\begin{aligned}
& \left(h_{31} x+h_{32} y+h_{33}\right) x^{\prime}-\left(h_{11} x+h_{12} y+h_{13}\right)=0 \\
& \left(h_{31} x+h_{32} y+h_{33}\right) y^{\prime}-\left(h_{21} x+h_{22} y+h_{23}\right)=0
\end{aligned}
$$

- Create a new system Ah = 0

Each point constraint gives two rows of $A$

$$
\left[\begin{array}{ccccccccc}
{[-x} & -y & -1 & 0 & 0 & 0 & x x^{\prime} & y x^{\prime} & x^{\prime} \\
0 & 0 & 0 & -x & -y & -1 & x y^{\prime} & y y^{\prime} & y^{\prime}
\end{array}\right]
$$

- Solve with singular value decomposition of $\mathrm{A}=\mathrm{USV}^{\top}$
- solution is in the nullspace of A мvDIARessean the last column of V (= last row of $\mathrm{V}^{\top}$ )
$\frac{\left[\begin{array}{c}w x^{\prime} \\ w y^{\prime} \\ w\end{array}\right]}{\mathbf{p}^{\prime}}$
from numpy import *

```
# create 4 random homogen. points %ythOn test COOQ
X = ones([3,4]) # the points are on columns
X[:2,:] = random.rand(2,4) # first row x coord, second y coord, third w = 1
X,Y = X[0],X[1]
# create projective matrix
H = random.rand( 3, 3)
# create the target points
Y = dot(H,X)
# homogeneous division
YY = (Y / Y[2])[:2,:]
u,v = YY[0],YY[1]
A = zeros([8,9])
for i in range(4):
    A[2*i ] = [-x[i], -y[i], -1, 0, 0, 0, x[i] * u[i], y[i] * u[i], u[i]]
    A[2*i+1] = [ 0, 0, 0, -x[i], -y[i], -1, x[i] * v[i], y[i] * v[i], v[i]]
[u,s,vt] = linalg.svd(A)
# reorder the last row of vt to 3x3 matrix
HH = vt[-1,:].reshape([ 3, 3])
# test that the matrices are the same (within a multiplicative factor)
print H - HH * (H[2,2] / HH[2,2])
```


## Summary of perspective stitching



- Pick one image, typically the central view (red outline)
- Warp the others to its plane
- Blend


## Example



## Using 4 shots instead of 3

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## Back to 3 shots


cylindrical reprojection

## Back to 3 shots


cylindrical reprojection

## Back to 3 shots


perspective reprojection

## Cylindrical panoramas

- What if you want a $360^{\circ}$ panorama?

- Project each image onto a cylinder
- A cylindrical image is a rectangular array


## Cylindrical panoramas

- What if you want a $360^{\circ}$ panorama?

- Project each image onto a cylinder
- A cylindrical image is a rectangular array
- To view without distortion
- reproject a portion of the cylinder onto a picture plane representing the display screen


## $2^{\text {nd }}$ reprojection to a plane for display



Imagine photographing the inside of a cylinder that is wallpapered with this panorama

- if your FOV is narrow, your photo won't be too distorted


## Demo



## Changing camera center

- Does it still work?


## Where to rotate? Nodal point?

- http://www.reallyrightstuff.com/pano/index.html


If you aim a ray at one of the nodal points, it will be refracted by the lens so it appears to have come from the other, and with the same angle with respect to the optical axis


## Rotate around center of lens perspective

- Many instructions say rotate around the nodal point
- wrong! http://toothwalker.org/optics/ misconceptions.html\#m6
- Correct: the entrance pupil
- the optical image of the physical aperture stop
 as 'seen' through the front of the lens
- due to the magnifying effect of the front lens, the entrance pupil's location is nearer than that of the physical aperture



## Test for parallax



Figure 3. Configuration to reveal the presence or absence of parallax. The subject is first placed at the left side of the frame, and subsequently at the right side after rotation of the camera about a vertical axis with the help of a panoramic tripod head.

http://toothwalker.org/optics/cop.html\#stitchin

## Correct center of rotation $\rightarrow$ no parallax



Figure 4. Rotation about an axis through the entrance pupil.


Figure 5. Rotation about an axis through the front nodal point.

## Cylindrical projection



- Map 3D point (X,Y,Z) onto cylinder

$$
(\hat{x}, \hat{y}, \hat{z})=\frac{1}{\sqrt{X^{2}+Z^{2}}}(X, Y, Z)
$$

- Convert to coordinates on unit cylinder
- $\operatorname{Conv}(\sin \theta, h, \cos \theta)=(\hat{x}, \hat{y}, \bar{z})$ es on unwrapped cylinder

```
(\tilde{x},\tilde{y})=(f0,fh)+(\mp@subsup{\tilde{x}}{c}{},\mp@subsup{\tilde{y}}{c}{})
```

Cylindrical projection


Focal length affects warping

top-down view


Image $384 \times 300$


Focal length

f = 180 (pixels)

$\mathbf{f}=\mathbf{2 8 0}$

$\mathrm{f}=\mathbf{3 8 0}$

## Focal length is (very!) camera dependent

- Can get a rough estimate by measuring the FOV:
- if the sensor size is known...

- Can use the EXIF tag
- might not give the correct value
- Can use several images together
- find $f$ that makes them match
- Etc.


## Assembling the panorama



Stitch pairs together, blend, then crop

## Problem: Drift



- Vertical Error accumulation
- small (vertical) errors accumulate over time
- apply correction so that sum $=0$ (for $360^{\circ}$ panorama)
- Horizontal Error accumulation
- can reuse first/last image to find the right panorama radius


## Spherical projection



- Map 3D point (X,Y,Z) onto sphere

- Convert to spherical coordinates
$(\sin \theta \cos \phi, \sin \phi, \cos \theta \cos \phi)=(\hat{x}, \hat{y}, \hat{z})$
- Convert to spherical image coordinates
$(\tilde{x}, \tilde{y})=(f \theta, f \phi)+\left(\tilde{x}_{c}, \tilde{y}_{c}\right)$


## Spherical Projection



## Building a Panorama

We need to match (align) images


## Detect feature points in both images

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## Find corresponding pairs

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## Use these pairs to align images



## Matching with Features

- Problem 1:
- Detect the same point independently in both images

no chance to match!


## We need a repeatable detector

## Matching with Features

- Problem 2:
- For each point correctly recognize the corresponding one



## We need a reliable and distinctive descriptor

## Harris Corners: The Basic Idea

- We should easily recognize the point by looking through a small window
- Shifting a window in any direction should give a large change in intensity


## Harris Detector: Basic Idea


"flat" region:
no change in all directions

"edge":
no change along the edge direction

"corner":
significant change in all directions

## Harris Detector: Mathematics

## Window-averaged change of intensity for the shift [u,v]:



Window function $\mathrm{w}(\mathrm{x}, \mathrm{y})=$


1 in window, 0 outside


Gaussian

## Harris Detector: Mathematics

Expanding $E(u, v)$ in a $2^{\text {nd }}$ order Taylor series expansion, we have, for small shifts [u,v], a bilinear approximation:

$$
E(u, v) \cong[u, v] M\left[\begin{array}{l}
u \\
v
\end{array}\right]
$$

where $M$ is a $2 \times 2$ matrix computed from image derivatives:

$$
M=\sum_{x, y} w(x, y)\left[\begin{array}{cc}
I_{x}^{2} & I_{x} I_{y} \\
I_{x} I_{y} & I_{y}^{2}
\end{array}\right]
$$

Eigenvalues $\lambda_{1}, \lambda_{2}$ of $M$ at different locations


Eigenvalues $\lambda_{1}, \lambda_{2}$ of $M$ at different locations


large $\lambda_{1}$, small $\lambda_{2}$

Eigenvalues $\lambda_{1}, \lambda_{2}$ of $M$ at different locations
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small $\lambda_{1}$, small $\lambda_{2}$

## Harris Detector: Mathematics

## Classification of image points using eigenvalues of M: <br> $\lambda_{2}$



## Harris Detector: Mathematics

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## Measure of corner

$$
M=\sum_{x, y} w(x, y)\left[\begin{array}{cc}
I_{x}^{2} & I_{x} I_{y} \\
I_{x} I_{y} & I_{y}^{2}
\end{array}\right]
$$

## response:

$$
R=\operatorname{det} M-k(\operatorname{trace} M)^{2}
$$

$$
\begin{aligned}
\operatorname{det} M & =\lambda_{1} \lambda_{2} \\
\operatorname{trace} M & =\lambda_{1}+\lambda_{2}
\end{aligned}
$$

(k - empirical constant, $\mathrm{k}=0.04-0.06$ )

## Harris Detector: Mathematics

- R depends only on eigenvalues of M
- $R$ is large for a corner
- $R$ is negative with large magnitude for an edge
- |R| is small for a flat region



## Harris Detector: Workflow



## Harris Detector: Workflow

Compute corner response $R$


## Harris Detector: Workflow

Find points with large corner response: $\mathrm{R}>$ threshold
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## Harris Detector: Workflow

Take only the points of local maxima of $R$

## Harris Detector: Workflow



## Harris Detector: Summary

- Average intensity change in direction $[u, v]$ can be expressed as a bilinear form:

$$
E(u, v) \cong[u, v] M\left[\begin{array}{l}
u \\
v
\end{array}\right]
$$

- Describe a point in terms of eigenvalues of $M$ : measure of corner response

$$
R=\lambda_{1} \lambda_{2}-k\left(\lambda_{1}+\lambda_{2}\right)^{2}
$$

- A good (corner) point snoura have a arge intensity change in all directions, i.e., $R$ should be large positive


## Harris Detector: Invariant to rotation



Ellipse rotates
but its shape (i.e., eigenvalues) remains the same
Corner response $R$ is invariant to image rotation

## Almost invariant to intensity change

- Partial invariance
$\checkmark$ Only derivatives are used

$$
=>
$$

invariance to intensity shift $\mathrm{I} \rightarrow \mathrm{I}+\mathrm{b}$
$\checkmark$ Intensity scale: I $\rightarrow$ a $\mid$


## Not invariant to image scale!



All points will be classified as edges

## Point Descriptors

- We know how to detect points
- Next question:

How to match them?


> Point descriptor should be:
> 1. Invariant
> 2. Distinctive

## SIFT - Scale Invariant Feature Transform



Figure 12: The training images for two objects are shown on the left. These can be recognized in a cluttered image with extensive occlusion, shown in the middle. The results of recognition are shown on the right. A parallelogram is drawn around each recognized object showing the boundaries of the original training image under the affi ne transformation solved for during recognition. Smaller squares indicate the keypoints that were used for recognition.

## SIFT - Scale Invariant Feature Transform

- Descriptor overview:
- Determine scale (by maximizing DoG in scale and in space), local orientation as the dominant gradient direction
- Use this scale and orientation to make all further computations invariant to scale and rotation

D. Lơvés. "Distinctive Image Features from Scale-Invariant Keypoints" IJCV 2004


## SIFT - Scale Invariant Feature Transform

- Descriptor overview:
- Determine scale (by maximizing DoG in scale and in space), local orientation as the dominant gradient direction
- Use this scale and orientation to make all further computations invariant to scale and rotation
- Compute gradient orientation histograms of several small windows (128 values for each point)
- Normalize the descriptor to make it invariant to intensity change

D. LƠPVes. Distinctive Image Features from Scale-Invariant Keypoints" IJCV 2004


## Registration in practice: tracking



## Viewfinder alignment for tracking



Andrew Adams, Natasha Gelfand, Kari Pulli
Viewfinder Alignment

## Project gradients along columns and rows

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ducrememinns
... diagonal gradients along diagonals ...
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... and find corners


Overlap and match the gradient projections


## Apply the best translation to corners



## Match corners, refine translation \& rotation



## System Overview



## System Overview



Hybrid multi-resolution registration
(1.B.) Image Based
F.B. Feature Based

E in


## Registration parameters

K. Pulli, M. Tico, Y. Xiong, X. Wang, C-K. Liang, "Panoramic Imaging System for Camera Phones", ICCE 2010

## Progression of multi-resolution registration

Actual size

Applied to hi-res

## Feature-based registration

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## System overview



## System overview



Photo by Marius Tico

## Image blending

- Directly averaging the overlapped pixels results in ghosting artifacts
- Moving objects, errors in registration, parallax, etc.


Photo by Chia-Kai Liang


## Solution: Image labeling

- Assign one input image each output pixel
- Optimal assignment can be found by graph cut [Agarwala et al. 2004]



## New artifacts

- Inconsistency between pixels from different input images
- Different exposure/white balance settings
- Photometric distortions (e.g., vignetting)



## Solution: Poisson blending

- Copy the gradient field from the input image
- Reconstruct the final image by solving a Poisson equation



## Seam finding is difficult when colors differ

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## System Overview



Photo by Marius Tico

## Panorama Visualization

- Trivial method:
- Show the whole panorama on the screen
- Zooming and panning



# No Projection Method is Optimal 



## Interpolate the Projection Coordinates




# Capturing and Viewing Gigapixel Images 

Johannes Kopf ${ }^{1,2}$<br>Matt Uyttendaele ${ }^{1}$<br>Oliver Deussen ${ }^{2}$<br>Michael Cohen ${ }^{1}$

1 Microsoft Research
2 Universität Konstanz

## BIG



Created from about 8008 MegaPixel Images

## BIG



## Wide


"Normal" perspective projections cause distortions.

## Deep



## High Dynamic Range

## Capture



## Capturing Gigapixel Images



## RAW



## DeVignette



## White Balance



## Exposure Balance



## Radiance Map

## Feature Points



## Feature Matches




## Radiometric Alignment



## Radiometric Alignment



Laplacian Blend

## Radiometric Alignment



## Poisson Blend

## Radiometric Alignment <br> 

Pure Radiometric

## Radiometric Alignment



## High Dynamic Range

## Tile Pyramid



## 272 Gigapixel Image Made Using 12,000 Photos from a Canon 7D

by ERIC REAGAN on JANUARY 14, 2011
in PHOTOGRAPHERS

## Passion for Photography?

Turn Your Passion into a Profession at The Art Institutes Online

## http://gigapan.org/gigapans/66e

 Aloeline $\begin{aligned} & \text { for }\end{aligned}$BLke164 people like this. Be the frst of your friends.


Photographer Alfred Zhao captured this 272 gigapixel image of the Shanghai skyline using the GigaPan EPIC Pro and a Canon 7 D with a $400 \mathrm{~mm} \mathrm{f} / 5.6$ lens and $2 \times$ teleconverter attached. He was setup and started shooting at around 8:30am and after 12,000 images were in the bag, it was just before dusk. It took months to complete image and get the final 1.09 TB file uploaded.

Just how big is a 272 gigapixel image? 1 gigapixel $=1000$ megapixels $=1$ billion pixels. That's 272 BILLION pixels. Printed at standard resolution, this image would cover over 7000 billboards.

But now it's done and Zhao holds a world record for the largest digital photo. There's no time to rest though, as Zhao says, "This is not the end of my panorama journey, it is a new start, challenging the limit is an infinite process. New records will appear in the future, it is only a matter of time."

## Optimizing Content-Preserving Projections for Wide-Angle Images

Robert Carroll University of California, Berkeley



Perspective
Mercator

Maneesh Agrawala University of California, Berkeley



Stereographic

Aseem Agarwala Adobe Systems, Inc.


Our Result

Figure 1: Wide-angle photographs can appear badly distorted under existing projections, such as the perspective, Mercator and stereographic projections. Perspective projection preserves linear structures in the scene, but distorts shapes of objects. Mercator and stereographic projections preserve shapes locally, but bend linear structures. Our projection is designed to both preserve local shape and maintain straight scene lines that are marked by the user with our interactive tool.

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## Push broom / slit scan panoramas

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## Photographing long scenes with multi-viewpoint panoramas

Aseem Agarwala ${ }^{1} \quad$ Maneesh Agrawala $^{4} \quad$ Michael Cohen $^{3} \quad$ David Salesin ${ }^{1,2}$ Rick Szeliski ${ }^{3}$



Abstract
We present a system for producing multi-viewpoint panoramas of long, roughly planar scenes, such as the facades of buildings along a city street, from a relatively sparse set of photographs captured with a handheld still camera that is moved along the scene. Our work is a significant departure from previous methods for creating multi-viewpoint panoramas, which composite thin vertical strips from a video sequence captured by a translating video camera, in that the resulting panoramas are composed of relatively large regions of ordinary perspective. In our system, the only user input required beyond capturing the photographs themselves is to identify the dominant plane of the photographed scene; our system then computes a panorama automatically using Markov Random Field optimization. Users may exert additional control over the appearance of the result by drawing rough strokes that indicate various high-level goals. We demonstrate the results of our system on several scenes, including urban streets, a river bank, and a grocery store aisle.

